

with increasing panel length to width ratio. The occurrence of single degree of freedom flutter, its experimental definition and theoretical prediction, remains one of the important problems in panel flutter. A detailed discussion is not possible here, but the reader is referred to Refs 8-11 for the literature on the subject.

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## Optical-Acoustic Effects in Solid Films

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**Acoustics effects of light radiation on solid film are noted, and a measurement method is described. Acetylene soot, camphor soot, flat black paper, glass, white paper, aluminum, and blackbody cavities were investigated. Proposed uses are noted.**

**O**PTICAL-ACOUSTIC effects were noted in gases in 1881. Recently, several Soviet investigators were concerned with different spectral regions and measurement methods in gases.<sup>2-6</sup> In some of our studies on diffusivity, similar optical-acoustic effects have been found in solid films. In the system used in this investigation (Fig. 1) the specimens were irradiated with a xenon gas phototube which puts out 1 megalumen for 1 msec. The acoustic pickup was a microphone with a flat response from 60 to 13,000 cps.

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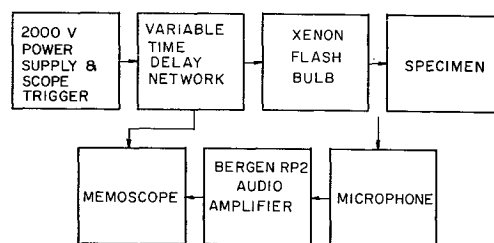


Fig. 1 Flash and audio system

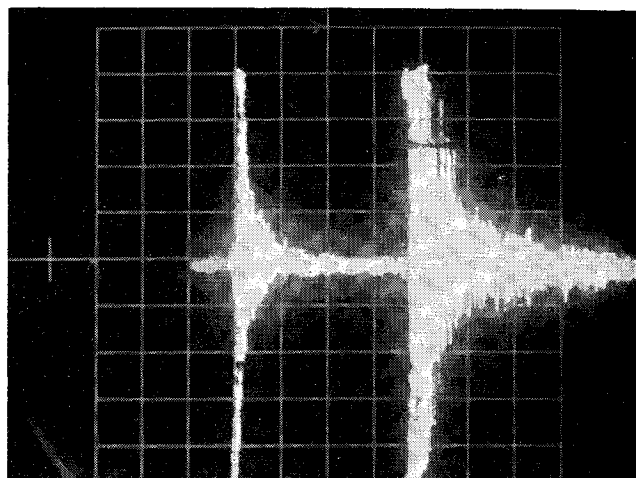


Fig. 2 Photograph of scope trace

Very sharp audible pulses were noted from acetylene soot covering on both electrical conductors and nonconductors. Less sharp reports were obtained from camphor soot and a very small noise from the flat black paper. White paper and various transparent plastics gave no report at all. The report given off by the black materials apparently is due to air motion following energy absorption.

In the use of uncoated aluminum sheet, no effect was noted for plates over 1 cm in thickness. Very thin aluminum sheets gave out a high pitched tone when irradiated. This effect appears to be due to light radiation pressure. Figure 2 shows the scope trace for acetylene soot. The left-hand pulse is relay noise obtained by closing the relay when the specimen is not irradiated, and the right-hand grouping is due to the combination of this same relay and the audible report due to energy absorption. This is a second sweep obtained when the horizontal sweep is moved and the specimen is irradiated. The sweep speed was 20 msec per division, and the vertical scale was 1 v per division. Reversing the acetylene coated glass so that the uncoated side is to the light stops the noise, thus indicating that the effect is beyond  $27\ \mu$  because the glass is not transparent beyond that point.

In this case, the light pressure or the formation of gas between the glass and the coating was sufficient to blow the coating off of the glass. Measurements from force transducers behind the specimen were inconclusive since several types of transducers appeared to be sensitive to the electrical transients in the circuit. Measurements of blackbody cavities gave results similar to the acetylene soot.

It is proposed that the order of magnitude of thermal absorptivity of nearly black specimens may be evaluated by a comparison of the magnitude of the acoustic energy released upon irradiation with the flash bulb. Extensive study would appear to be required if high accuracy were to be obtained.

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## Turbulent Wake Characteristics with Different Eddy Viscosity Coefficients

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IN the studies of turbulent hypersonic wakes, the viscosity coefficient for laminar wake is generally replaced by an eddy viscosity coefficient. The forms of the eddy viscosity coefficient assumed in various theories<sup>1-5</sup> may be classified into three general types. They are

$$\mu_{e1} = K_1 \delta (\rho_e u_e - \rho u) \quad (1)$$

$$\mu_{e2} = K_2 \delta \rho (u_e - u) \quad (2)$$

$$\mu_{e3} = K_3 \delta \rho (u_e - u) \quad (3)$$

where the  $K$ 's are constants to be assumed. All these three forms of the eddy viscosity coefficients reduce to the same expression generally used in the incompressible turbulent free-mixing problem, i.e.,  $K_i \rho_i \delta_i (u_i - u)$ .

This note gives and compares some numerical results of the equilibrium turbulent-wake characteristics obtained by using these three different forms of the eddy viscosity coefficients with the governing equations, method of calculations, and initial and boundary conditions being the same for all three cases.

To simplify the analysis, the usual wake equations of the boundary-layer type approximation are further reduced by assuming the Lewis number and the Prandtl number equal to one, and the axial pressure gradient as negligible. The governing equations are, then, in axisymmetric coordinates

$$\frac{\partial(\rho u)}{\partial x} + \frac{1}{r} \frac{\partial(\rho v r)}{\partial r} = 0 \quad (4)$$

$$\rho u \frac{\partial u}{\partial x} + \rho v \frac{\partial u}{\partial r} = \frac{1}{r} \frac{\partial}{\partial r} \left( r \mu_e \frac{\partial u}{\partial r} \right) \quad (5)$$

$$\rho u \frac{\partial h}{\partial x} + \rho v \frac{\partial h}{\partial r} = \mu_e \left( \frac{\partial u}{\partial r} \right)^2 + \frac{1}{r} \frac{\partial}{\partial r} \left( r \mu_e \frac{\partial h}{\partial r} \right) \quad (5a)$$

It is well known that the following relation holds in this case, i.e.,

$$h + (u^2/2) = A + Bu \quad (6)$$

where  $A$  and  $B$  are constants. If the initial condition also satisfies (6), then this relation between the enthalpy and the velocity is valid for the whole viscous flow regime. It remains now to solve Eq. (5).

To do this, the integral method is employed. The integration of Eq. (5) from  $r = 0$  to  $r = \delta$  gives

$$\frac{d}{dx} \left[ \rho u^2 \delta^2 \int_0^1 \frac{\rho u}{\rho u_e} \left( \frac{u}{u_e} - 1 \right) \frac{r}{\delta} d \left( \frac{r}{\delta} \right) \right] = 0 \quad (7)$$

where Eq. (4) and assumption  $du/dx \cong 0$  have been used, and the boundary conditions  $\partial u / \partial r = 0$  at  $r = 0$  and  $r = \delta$  have been enforced. Equation (7) can then be rewritten as

$$\rho u^2 \delta^2 \theta = \text{const} \quad (7a)$$

where

$$\theta = \int_0^1 \frac{\rho u}{\rho u_e} \left( \frac{u}{u_e} - 1 \right) \frac{r}{\delta} d \left( \frac{r}{\delta} \right) = \int_0^1 \frac{\rho u}{\rho u_e} \left( \frac{u}{u_e} - 1 \right) \eta d\eta$$

The momentum balance along the axis gives another condition as

$$\left[ \rho u \left( \frac{\partial u}{\partial x} \right) \right]_{=0} = \left( 2 \mu_e \frac{\partial^2 u}{\partial r^2} \right)_{=0}$$

It can be shown that this is equivalent (see Ref. 6), in non-dimensional form, to

$$\left( \bar{\rho} \bar{u} \frac{\partial \bar{\rho} \bar{u}}{\partial \bar{x}} \right)_{\eta=0} = \left( \frac{\mu_e}{\rho u \delta_0} \frac{2 \bar{\mu}_e}{\bar{\delta}^2} \frac{\partial^2 \bar{\rho} \bar{u}}{\partial \eta^2} \right)_{\eta=0} \quad (8)$$

where  $\bar{\rho} = \rho / \rho_0$ ,  $\bar{u} = u / u_0$ ,  $\bar{\mu}_e = \mu_e / \mu_0$ ,  $\bar{x} = x / \delta_0$ ,  $\bar{\delta} = \delta / \delta_0$  and  $\delta_0$  is the initial viscous wake radius.

Now, the following profile for  $\bar{\rho} \bar{u}$  is assumed,

$$\bar{\rho} \bar{u} = F(\eta) + a[1 - F(\eta)] \quad (9)$$

where  $F(\eta)$  is the given initial profile for  $\bar{\rho} \bar{u}$  at  $x = 0$ . Substituting (9) into (8) results in

$$\frac{da}{d\bar{x}} = \frac{\mu_e}{\rho u \delta_0} \frac{2 \bar{\mu}_e}{\bar{\delta}^2} \frac{F_0''(1-a)}{(1-F_0)[F_0 + a(1-F_0)]} \quad (10)$$

where  $F_0 = F(0)$  and  $F_0'' = (\partial^2 F / \partial \eta^2)_{\eta=0}$ . The solution of Eqs. (10) and (7a) yields  $\bar{\delta}$  and  $a$  as functions of  $\bar{x}$  and hence the distribution of  $\bar{\rho} \bar{u}$ . With the thermodynamic relation  $\rho = f_1(h, p)$  or  $h = f_2(p, \rho)$  and relation (6),  $\bar{h}$  and  $\bar{u}$  can be calculated. The wake characteristics in the whole field can then be obtained.

To study the effect of the different eddy viscosity coefficients given in (1-3) on the wake characteristics, it remains to substitute these coefficients into (10) in turn, and obtain the solution for the individual case using the same initial and boundary conditions.

This has been applied to the case of a slender cone at altitude = 150,000 ft and  $M_\infty = 19.52$ . The external inviscid flow conditions were assumed uniform. The initial flow profiles used in the calculations are shown in Fig. 1. It is noted that the peak enthalpy is located off the axis for the initial profiles so assumed. The results of the variations of the centerline enthalpy  $\bar{h}$  with  $2K\bar{x}$  for the three cases are shown in Fig. 2, and those of the centerline velocity  $\bar{u}$  and the eddy viscosity coefficient  $\bar{\mu}_e'$  in Fig. 3.

From Fig. 2, it is seen that the distance which the off-axis peak enthalpy takes to reach the axis differs significantly

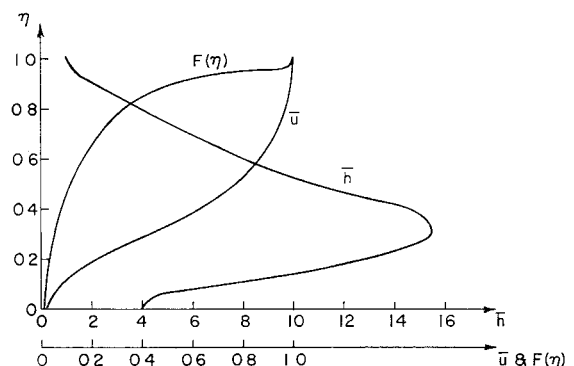


Fig. 1 The initial profiles; slender cone, altitude = 150,000 ft,  $M_\infty = 19.52$

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